

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

| CANDIDATE NAME | | |
|---|---|--|
| CENTER NUMBER | | CANDIDATE NUMBER |
| MATHEMATICS | 5 (US) | 0444/31 |
| Paper 3 (Core) | | May/June 2016 |
| | | 2 hours |
| Candidates ans | wer on the Question Paper. | |
| Additional Mater | rials: Geometrical instrume Electronic calculator | |
| READ THESE I | NSTRUCTIONS FIRST | |
| Write in dark blu You may use an Do not use stap | | |
| Electronic calculate of three significant Give answers in | d for any question it must be s lators should be used. accuracy is not specified in the | e question, and if the answer is not exact, give the answer to |
| | points is given in parentheses points for this paper is 104. | [] at the end of each question or part question. |
| Write your calc | culator model in the box belo | ow. |
| | | |

This document consists of 16 printed pages.



[Turn over

Formula List

| Area, A , of triangle, base b , height h . | $A = \frac{1}{2}bh$ |
|--|--------------------------|
| Area, A , of circle, radius r . | $A=\pi r^2$ |
| Circumference, C , of circle, radius r . | $C = 2\pi r$ |
| Lateral surface area, A , of cylinder of radius r , height h . | $A=2\pi rh$ |
| Surface area, A , of sphere of radius r . | $A=4\pi r^2$ |
| Volume, V , of prism, cross-sectional area A , length l . | V = Al |
| Volume, V , of cylinder of radius r , height h . | $V = \pi r^2 h$ |
| Volume, V , of sphere of radius r . | $V = \frac{4}{3}\pi r^3$ |

| 1 | (a) | 3 | 6 | 19 | 20 | 24 | 27 | 30 | 32 | 35 | 36 | 48 | 49 | 72 | |
|---|-----|-------|--------------------|-----------|----------|-----------|-----------|----------|--------|------|----|-------|----|----|-------|
| | | Fro | m this | list of r | numbers | s write c | lown | | | | | | | | |
| | | (i) | a fac | tor of 1 | 5, | | | | | | | | | | [1] |
| | | (ii) | a mu | ltiple of | f 18, | | | | | | | | | | [1] |
| | | (iii) | an oc | ld squai | re numb | oer, | | | | | | | | | [1] |
| | | (iv) | a cub | e numb | oer, | | | | | | | | | | [1] |
| | | (v) | the c | ube roo | t of 216 |). | | | | | | | | | [1] |
| | (b) | Wri | te as a | percen | tage. | | | | | | | | | | |
| | | (i) | 0.43 | | | | | | | | | | | | |
| | | (ii) | $\frac{1}{2}$ | | | | | | | | | | | | % [1] |
| | | | | | | | | | | | | ••••• | | | % [1] |
| | (c) | Wri | te $\frac{28}{42}$ | in its lo | west te | rms. | | | | | | | | | |
| | | | | | | | | | | | | | | | [1] |
| | (d) | (i) | Write | e 45 as a | a produ | ct of its | prime f | factors. | | | | | | | |
| | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | [2] |
| | | (ii) | Find | the grea | atest co | mmon f | factor (C | GCF) of | 45 and | 105. | | | | | |
| | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | [2] |

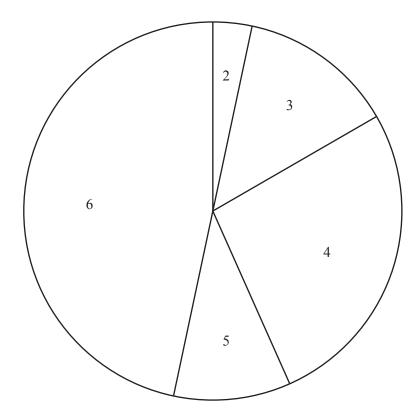
| Joe | Joel spins a fair five-sided spinner numbered 2, 3, 4, 5 and 6. | | | | | | | | | | | | | |
|-----|---|----------------|---------|----------|----------|----------|----------|---------|----------|--------|-------|--------|--------|-----|
| (a) | Wri | te down tl | he prob | oabilit | y that 1 | the spin | nner la | ınds on | 1 | | | | | |
| | (i) | an odd number, | | | | | | | | | | | | |
| | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | [1] |
| | (ii) | a prime | numbe | er, | | | | | | | | | | |
| | | | | | | | | | | | •••• | | | [1] |
| | (iii) | the num | ber 7. | | | | | | | | | | | |
| | () | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | [1] |
| (b) | Цог | e are the r | ·aculta | of his | first 2 | 0 anina | | | | | | | | |
| (D) | 1101 | e are the r | | | | | | | | | | | | |
| | | | 2 | 2 5 | | 3 5 | 3 | | 4 6 | 4 6 | | 4 6 | | |
| | | | 4 | 3 | 3 | 3 | 3 | U | O | U | Ü | O | | |
| | (i) | Write do | own the | e mod | e. | | | | | | | | | |
| | | | | | | | | | | | | | | [1] |
| | (ii) | Calculat | e the n | nean. | | | | | | | | | | |
| | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | [2] |
| | (888) | T 1 | | | | | | | •. | | ••••• | | •••••• | [2] |
| | (iii) | Joel war | | | - | | | | | | | | | |
| | | (a) Sho | ow that | t the so | ector a | ngle fo | or the r | numbei | r 2 is 5 | 4°. | | | | |
| | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | [1] |
| | | (b) Fin | d the s | sector | angle f | for the | numbe | er 6. | | | | | | |
| | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | |

.....[2]

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(c) Joel asks 30 students to guess the number that the spinner will next land on. The results are shown in this pie chart.



| (i) | The sector angle for the number 6 is 168° | ٥. |
|-----|---|----|
| | | |

How many students guessed the number 6?

| [|
|---|
|---|

(ii) Find the percentage of the students who guessed a number less than 5.

.....% [3]

(iii) Joel spins the spinner. 10% of the 30 students guessed correctly.

Which number did the spinner land on?

.....[2]

| Pau | l and Mary go on a 14 night cruise in the Mediterranean. | |
|-----|---|-------|
| (a) | The price of the cruise is \$237 per person per night. A tax of 6% is added to this price. | |
| | Find the total amount Paul and Mary pay for this cruise. | |
| | | |
| | | \$[3 |
| (b) | At a port Mary buys 2 bottles of sun cream. Each bottle costs \$7.89. | |
| | Work out the change she receives from \$20. | |
| | | \$ [2 |
| | | Ψ[4 |
| (c) | Paul and Mary leave the ship at 0923 to tour Pisa. The tour lasts for $6\frac{3}{4}$ hours. | |
| | Find the time when the tour finishes. | |
| | | |
| | | [2 |
| (d) | The ship leaves at 1840 to sail to the next port. It sails 270 km at an average speed of 32.4 km/h. | |
| | Find the time when the ship arrives. | |
| | | |
| | | |
| | | [3 |
| (e) | There are 1800 passengers on the ship. They are in the ratio males: females = 5:4. | |
| | Work out the number of male passengers. | |
| | | |
| | | |

.....[2]

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3

| | | | , |
|---|-----|------|---|
| 4 | (a) | Sol | ve these equations. |
| | | (i) | x + 7 = 15 |
| | | | |
| | | | x = [1] |
| | | (ii) | 5(3x+8) = 10 |
| | | | |
| | | | |
| | | | x = [3] |
| | (b) | Ac | lub is arranging transport for its members. |
| | | Spe | zedy Buses charge \$625 plus \$15 per member. |
| | | | e function $C(x) = 15x + 625$, where x is a positive integer, models the total cost, in dollars, of asport for x members. |
| | | (i) | Sporty Buses charge \$117 plus \$19 per member. |
| | | | Write a function that models the total cost in dollars, $D(x)$, where x is a positive integer, of transport for x members. |
| | | | |
| | | | |

$$D(x) =$$
 [2]

(ii) The total cost is the same for both Speedy Buses and Sporty Buses.

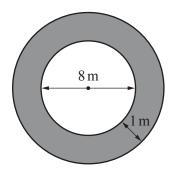
Write down an equation and solve it to find x.

5 (a) The table shows the temperature at noon each day for one week in a city.

| Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday |
|--------|---------|-----------|----------|--------|----------|--------|
| 5°C | 2°C | −3 °C | −1°C | 0°C | 1°C | −2°C |

| (i) | Which day had the lowest noon temperature? | |
|----------------|---|-----------|
| (ii) | | [1] y. |
| (iii) | | °C [1] |
| | lowest | [1] |
| (iv) | The next day the noon temperature fell by 4 °C. | |
| | Find the noon temperature on the next day. | |
| | | °C [1] |
| (b) The | e number of houses in the city is 1 935 364. | |
| (i) | Write this number correct to the nearest million. | |
| | | [1] |
| (ii) | There are approximately 6 078 000 people living in houses in the city. | |
| | Using your answer to part (b)(i), estimate the number of people per house. Give your answer to an appropriate level of accuracy. | |
| | | [2 |
| | | [4 |

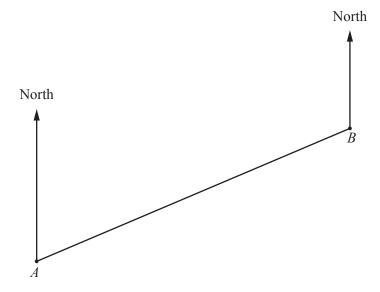
(c) The diagram shows the cross section of a circular tunnel in the city.



NOT TO SCALE

Calculate the shaded area.

6 (a) The scale drawing shows port *A* and port *B*. The scale is 1 centimeter represents 15 kilometers.



Scale: 1 cm to 15 km

A ship sails from port A to port B.

(i) Measure the bearing of port B from port A.

.....[1]

(ii) Find the actual distance from port A to port B.

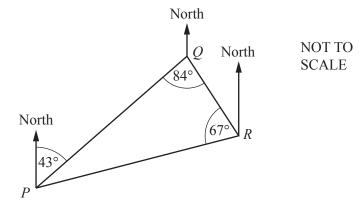
.....km [2]

(iii) The ship then sails from port B to port C. Port C is 90 km from port B on a bearing of 146°.

On the scale drawing mark the position of port *C*.

[2]

(b) Another ship sails from port *P* to port *Q*. It then sails from port *Q* to port *R* before returning to port *P*.



(i) Find angle RPQ.

| Angle $RPO =$ | [1] |
|---------------|---------|
| | |

(ii) Find the bearing of port P from port R.

.....[2]

North $\begin{array}{c|c}
T \\
\hline
356 \text{ km} \\
\hline
8 & -24 \text{ NOT TO} \\
\hline
267 \text{ km}
\end{array}$

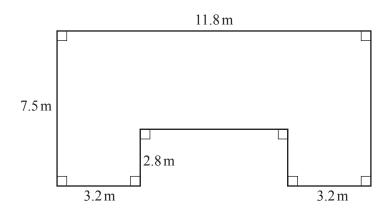
Port *T* is 267 km east and 356 km north of port *S*.

Calculate the distance ST.

 $ST = \dots km [2]$

7 Jared is building a house.

(a)



NOT TO SCALE

The diagram shows the plan of the floor of the house.

(i) Find the area of the floor.

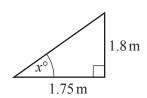
| | $m^{2}[3]$ |
|--|------------|
|--|------------|

(ii) For every square meter of floor area, it costs \$2175 to build the house.

Calculate the cost of building the house. Give your answer correct to 3 significant figures.

\$..... [2]

(b)



NOT TO SCALE

The diagram shows a section of the roof.

Using trigonometry, calculate the value of x.

x = [2]

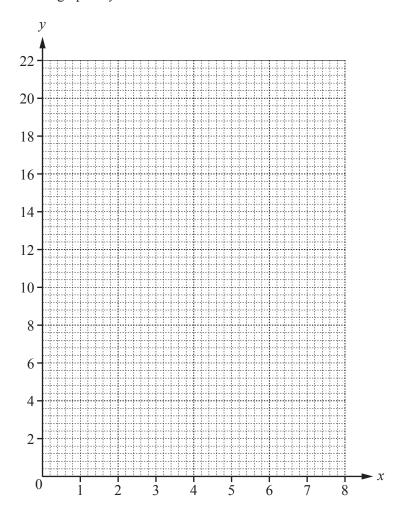
| (c) | Jared invests \$50 000 for three years at a rate of 2% per year compound interest. |
|-----|--|
| (0) | |
| | Calculate the total amount Jared receives at the end of the three years. |
| | |
| | |
| | |
| | |
| | |
| | |
| | ¢ [2 |
| | \$[3 |
| (d) | Jared also built an apartment for \$180 000. He sells it for \$198 000. |
| | Calculate the percentage profit that he makes. |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | % [3 |
| | |
| | |
| | |

8 (a) Complete the table of values for $y = 8 + 7x - x^2$.

| х | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|---|---|----|---|---|----|---|---|---|
| у | 8 | | 18 | | | 18 | | 8 | |

[3]

(b) On the grid, draw the graph of $y = 8 + 7x - x^2$ for $0 \le x \le 8$.



[4]

| (c) | Write down the co-ordinates of the highest point of the curve. |
|-----|--|
| | |

| | | | | | | | | | | | | | | | | | | | | | _ | | |
|---|--|--|--|--|--|--|--|--|--|---|--|--|--|--|--|--|--|--|---|----|---|---|---|
| 1 | | | | | | | | | | | | | | | | | | | 1 | ١. | Г | 1 | ı |
| ١ | | | | | | | | | | , | | | | | | | | | J | , | | 1 | ı |
| | | | | | | | | | | | | | | | | | | | | | | | |

(d) (i) On the grid, draw the line
$$y = 16$$
.

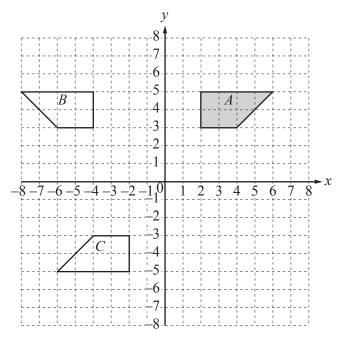
[1]

(ii) Use your line to solve the equation $8 + 7x - x^2 = 16$.

$$x =$$
 or $x =$ [2]

Question 9 is printed on the next page.

9



- (a) On the grid, draw the image of shape A after a translation by the vector $\begin{pmatrix} -2 \\ -6 \end{pmatrix}$. [2]
- **(b) (i)** On the grid, draw the image of shape A after an enlargement, scale factor 2, center (4, 4). [2]
 - (ii) Write down the scale factor of the enlargement that maps the image in **part** (b)(i) back onto shape A.

| 1 | ٦ |
|-------|---|
| 1 | 1 |

(c) Describe fully the **single** transformation that maps shape A onto shape B.

| [2] |
|---------|

(d) Describe fully the **single** transformation that maps shape A onto shape C.



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